

Lecture 20: Oct. 21, 2016.

- Housekeeping:
- HW 10 Weds. in class
  - Canvas quiz Mon. 11:59 p.m.

- Last time:
- Intro. parametric curves
  - Sketching — — —
  - Eliminating the parameter

# Parametrizing curves.

- The graph of any function  $y = f(x)$  has the "natural parametrization" 
$$\begin{cases} x = t \\ y = f(t) \\ t \in \text{domain}(f(x)) \end{cases}$$

EXAMPLE. Parametrization of the line through  $(a, b)$  with slope  $m$ .

Cartesian Equation:  $y - b = m(x - a) \Leftrightarrow y = mx + (b - ma)$

Natural Parametrization: 
$$\begin{cases} x = t \\ y = mt + (b - ma) \\ t \in \mathbb{R} \end{cases}$$

Another Parametrization: 
$$\begin{cases} x = \cancel{t}^2 \cdot 2t \\ y = 2mt^2 + (b - ma) \\ t \in \mathbb{R} \end{cases}$$

Yet Another Parametrization:

Let  $t := x - a$ . So 
$$\begin{cases} x = t + a \\ y = mt + b \\ t \in \mathbb{R} \end{cases}$$